

---

# Modeling the Fate and Transport of Engineered Nanoparticles in Porous Media

---

**Nadim Copty**

*Institute of Environmental Sciences*

*Bogazici University*

*Istanbul, Turkey*

*NM2PorousMedia, Dubrovnik, Croatia, Sept. 29-Oct. 3, 2014*



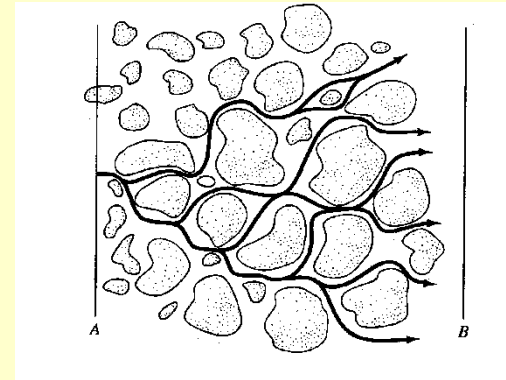
# Uses of Engineered Nanoparticles

---

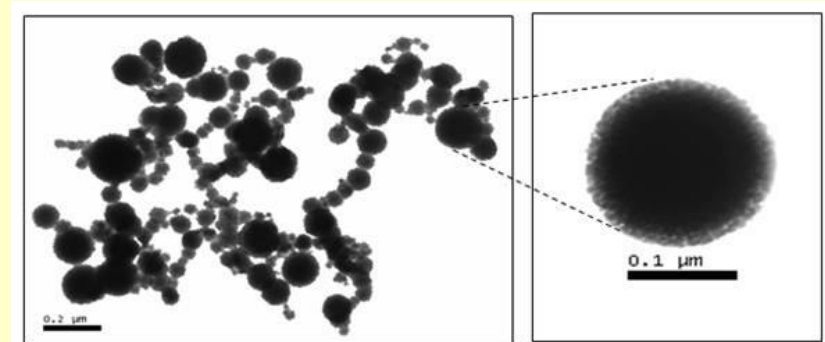
- Engineered nanoparticles are being used in a wide range of applications, such as cosmetics, paint, medical and electronic devices, and chemical catalyst.
- Increased use of engineered nanoparticles has raised concerns about their impact on human health and the environment, including possible contamination of surface and groundwater resources.
- Nanoparticles are also used in environmental applications, such as water and wastewater treatment and *in-situ* remediation of groundwater

# Engineered Nanoparticles for *In-Situ* Groundwater Remediation

- Engineered NP are injected into the subsurface with the goal of traveling to the zone of contamination where they react with the contamination.



- Advantages of using NP include their **high reactivity** due to their **large specific surface area** and their potential **ability to travel** to areas of contamination.

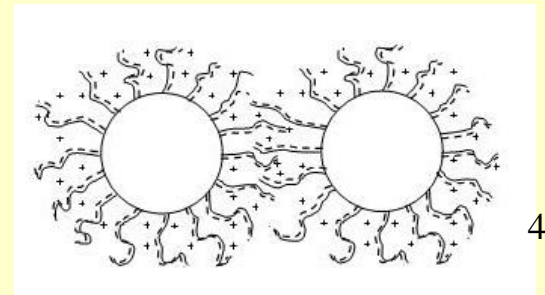


- Examples of Engineered NP:
  - Metal oxides ( $\text{Fe}_3\text{O}_4$  and  $\text{TiO}_2$ ) for the immobilization of heavy metals
  - nZVI for the degradation of halogenated hydrocarbons

# Challenges facing the use of Nanoparticles for *In-Situ* Groundwater Remediation

---

- A critical step for the development of such a technology is the **effective deliverability** of the NP suspension to the zone of contamination.
- Because of their relatively high surface energy, **bare nanoparticles may undergo significant aggregation** and deposition within the porous media, thereby limiting its transport.
- To enhance the mobility of engineered nanoparticle, **surface stabilization** with various materials have been considered: polymers, surfactants, starch.
- Surface coating provides steric and electrostatic repulsion forces between particles.



# Factors Influencing NP transport in Porous Media

---

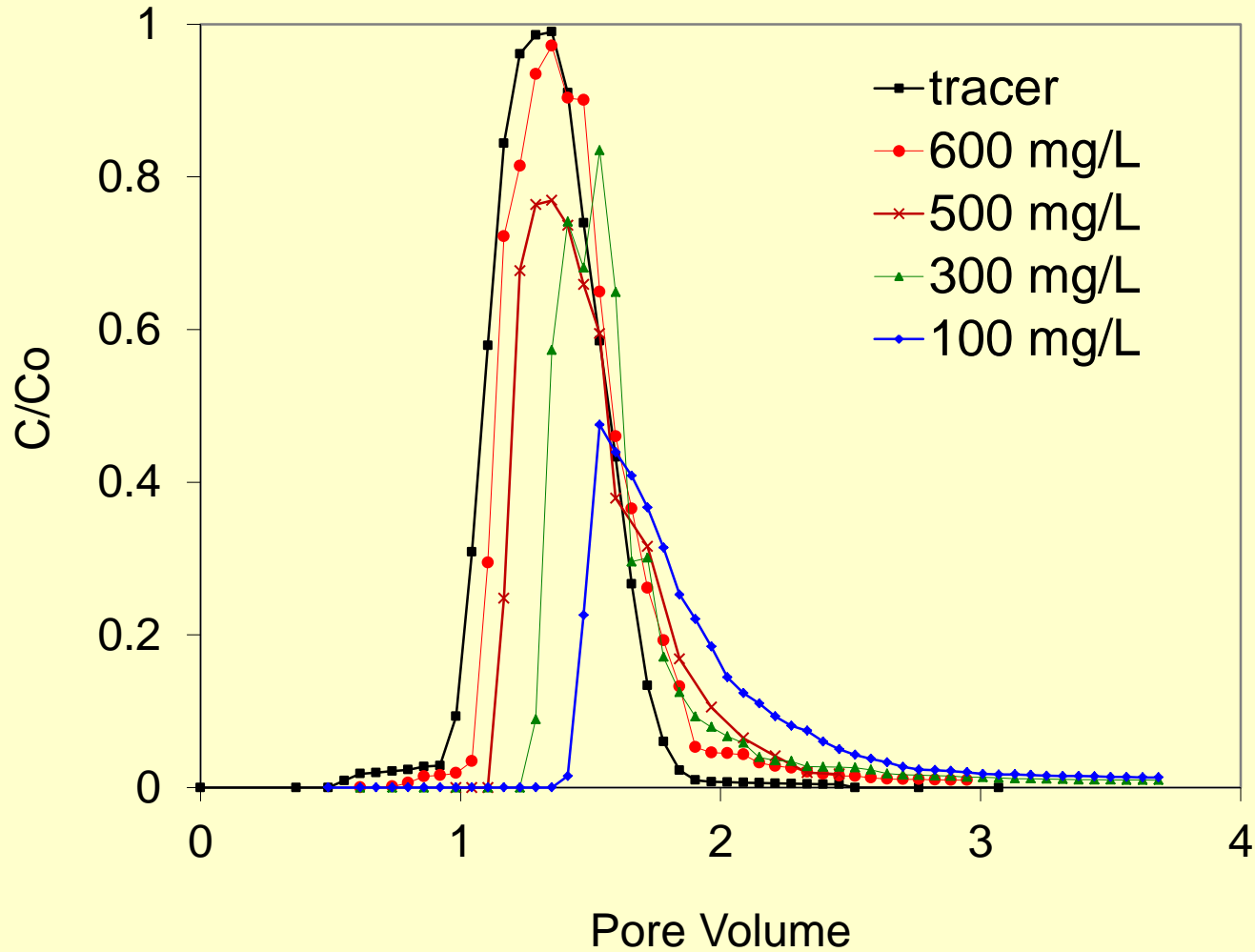
- Factors influencing NP transport in porous media include: particle size, velocity, fluid properties such as ionic strength and pH, and soil matrix properties
- In this study we examine the effect of nanoparticle **concentration** on its mobility.
- The nanoparticle considered in this study is poly(acrylic acid) (PAA) supported magnetite ( $\text{Fe}_3\text{O}_4$ ).

# Experimental setup

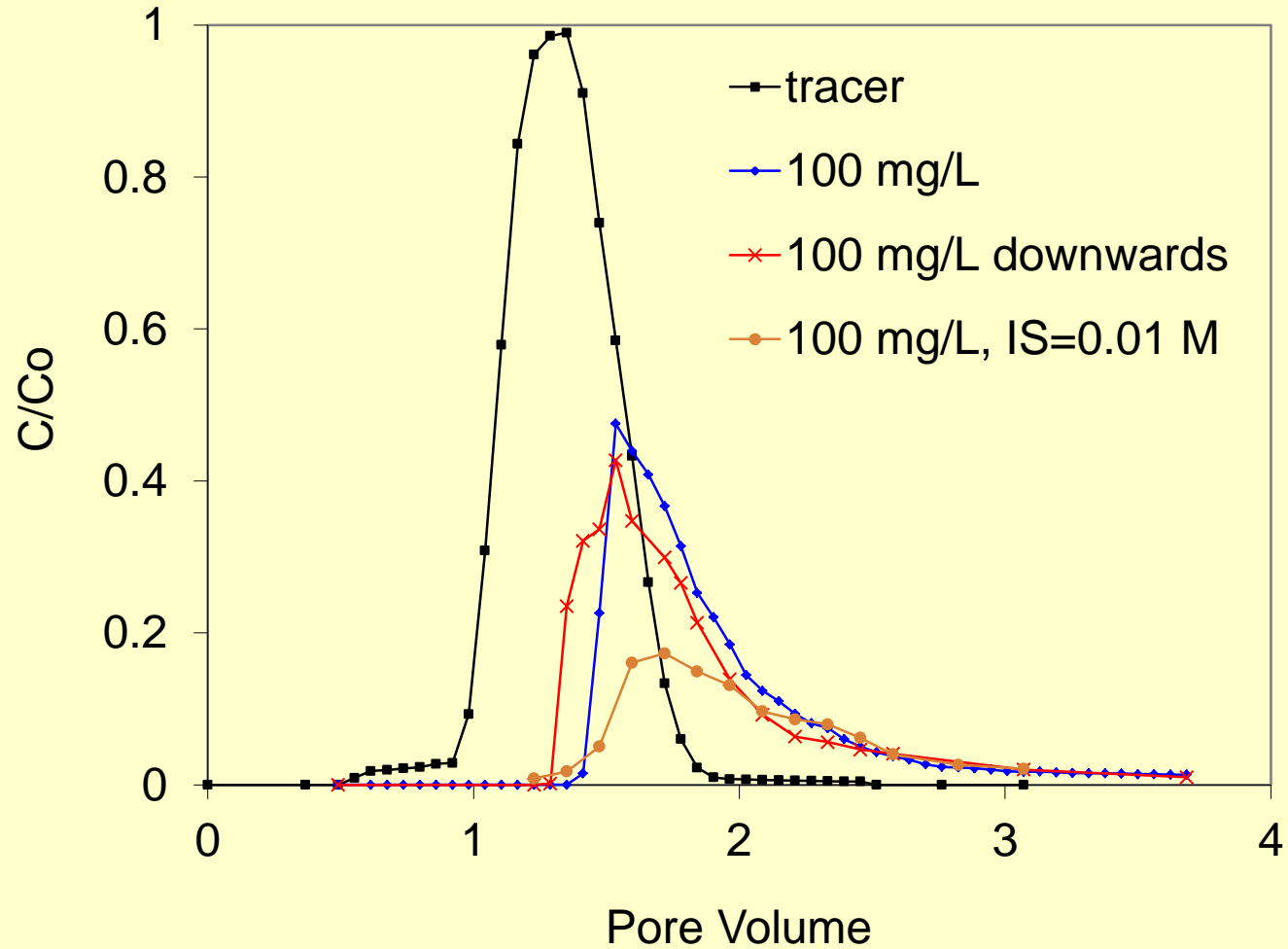
- Transport experiments were performed in a vertical glass column  $L=30$  cm and  $ID=4.8$  cm.
- Porous medium consisted of clean sand with mean grain diameter of 0.2 mm.
- Input Fe concentrations were varied between 100 and 600 mg/L.
- Flow rate was maintained constant for all experiments.
- In each transport experiment, 100 mL (about half the column pore volume) of the nanoparticle solution were fed into the column.
- Nanoparticle transport was also compared to the transport of a nonreactive trace.



# Normalized Eluted Concentration vs time

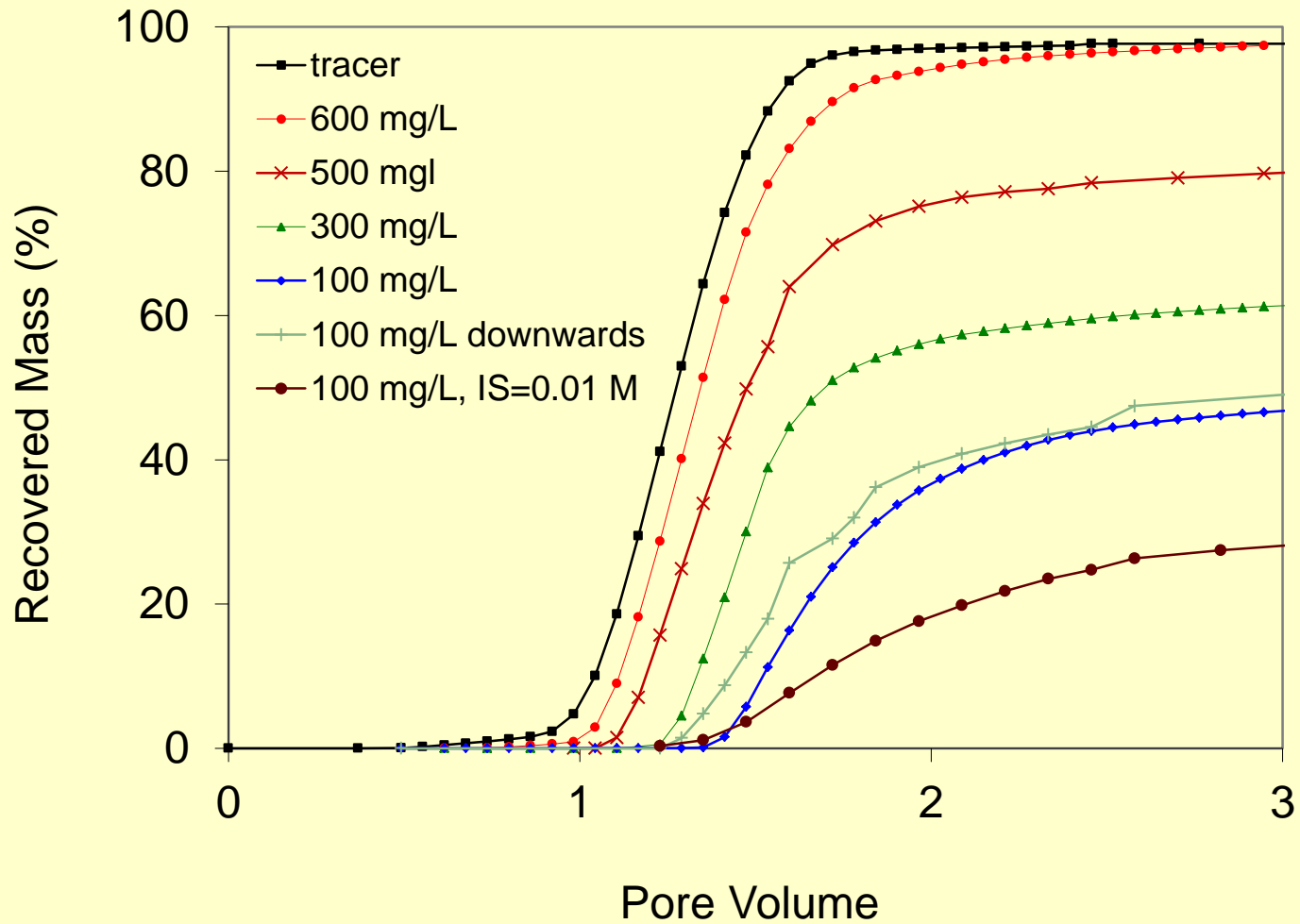


# Normalized Eluted Concentration vs time



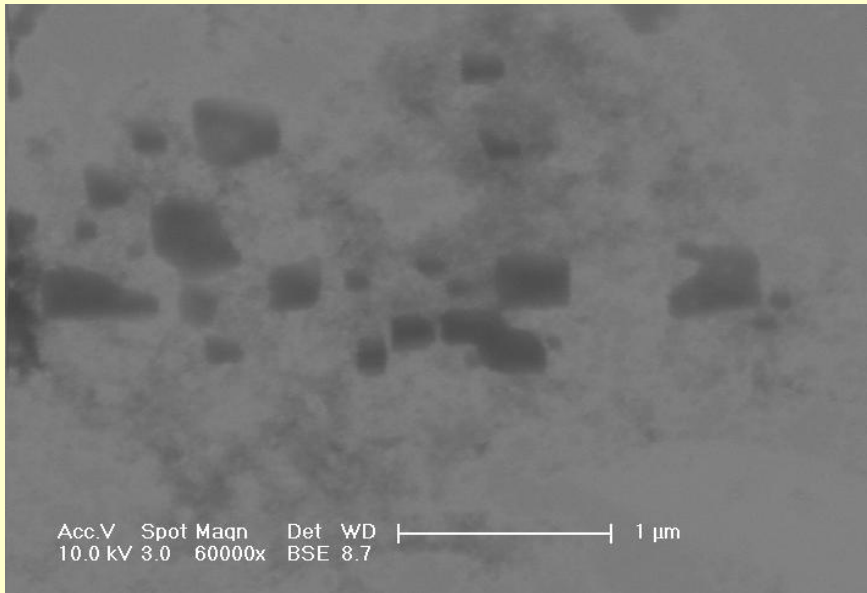


# Recovered NP Mass vs time

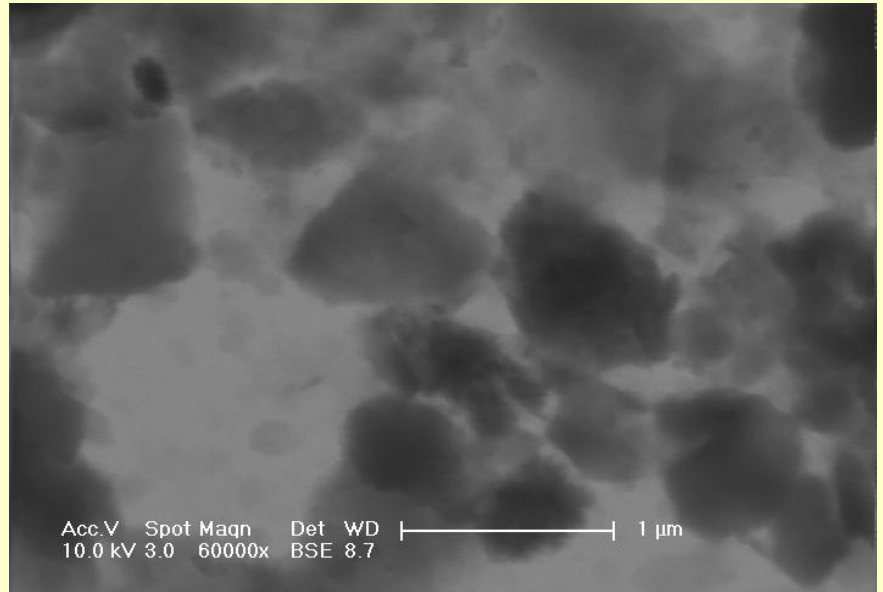


# Particle Size Distribution

---

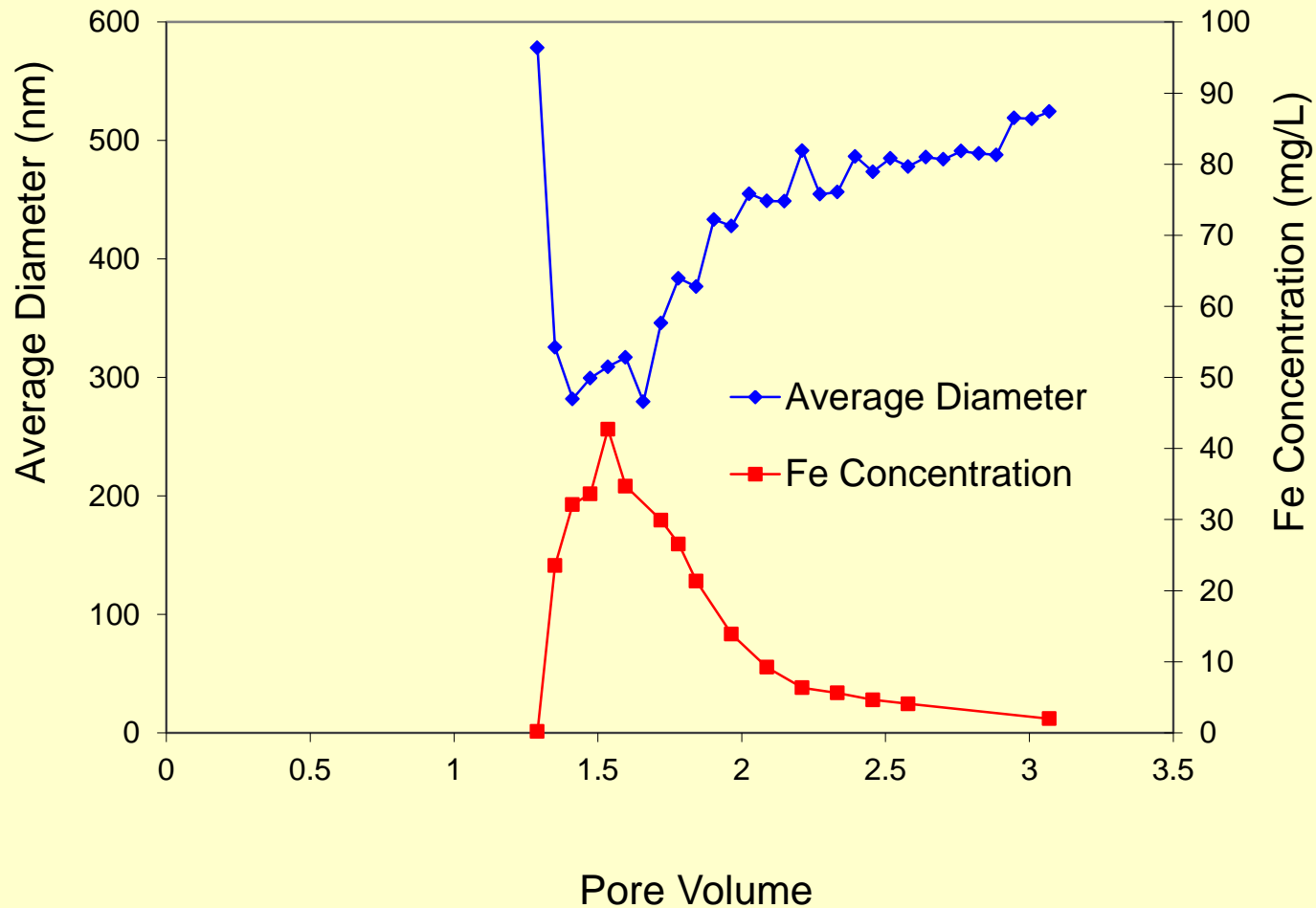


Injected Suspension



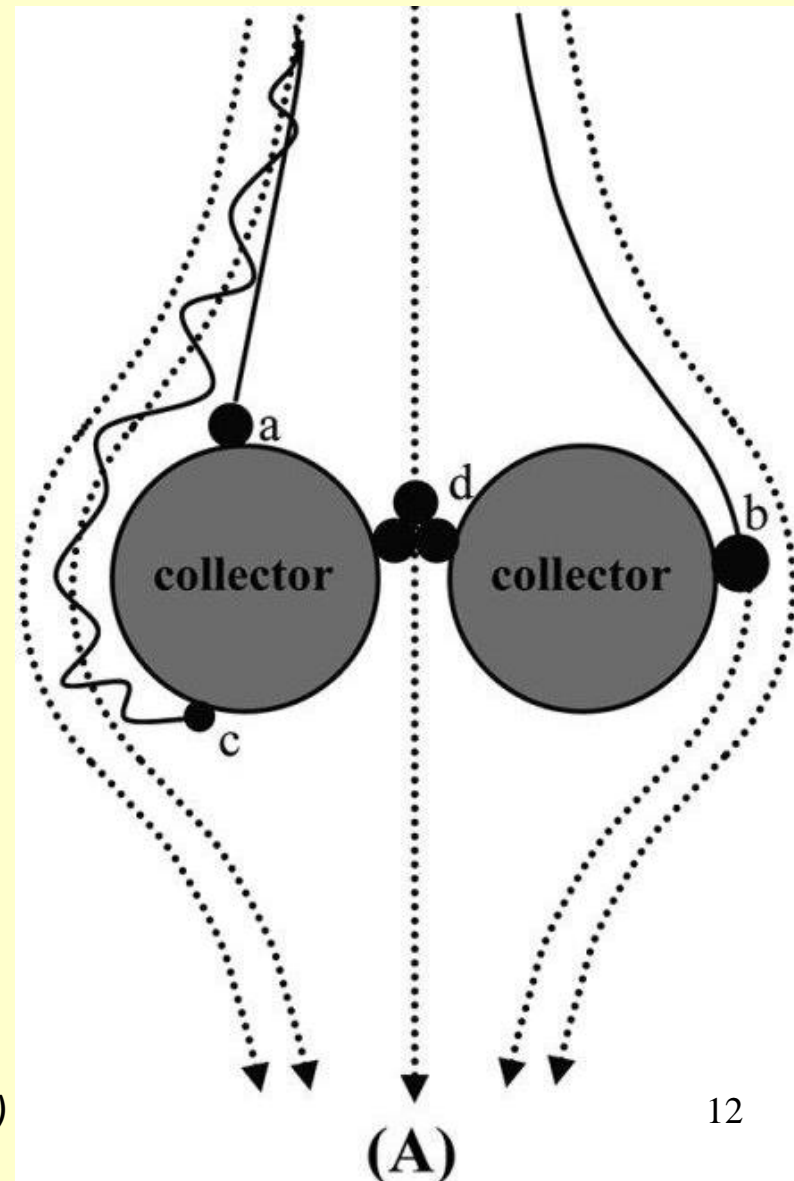
Eluted Suspension

# Eluted Concentration vs. Particle Size



# NP Retention in Porous Media

- gravitational sedimentation (a)
- Interception (b)
- Brownian diffusion (c)
- Aggregation and physical retention in small pores, also called straining (d)



# NP Transport Model

---

- Advection-Dispersion Equation

$$\frac{\partial C}{\partial t} = -v \frac{\partial C}{\partial x} + D \frac{\partial^2 C}{\partial x^2} - r_{dep}$$

- net particle deposition/detachment rate term

$$r_{dep} = \rho_b \frac{\partial S}{\partial t} = nK_{dep}\psi C - \rho_b K_{det} S$$

$$\psi = (1 - S/S_{max})$$

- The above non-linear differential equation was solved using the total-variation-diminishing (TVD) method

# NP Deposition/Detachment Model Options

---

1. kinetic deposition and detachment terms but no blocking (large  $S_{\max}$ ):

➤ Best-fit parameters are  $K_{\text{dep}}$  and  $K_{\text{det}}$

2. kinetic deposition term with blocking but no detachment ( $K_{\text{det}} = 0$ ):

➤ Best-fit parameters are  $K_{\text{dep}}$  and  $S_{\max}$

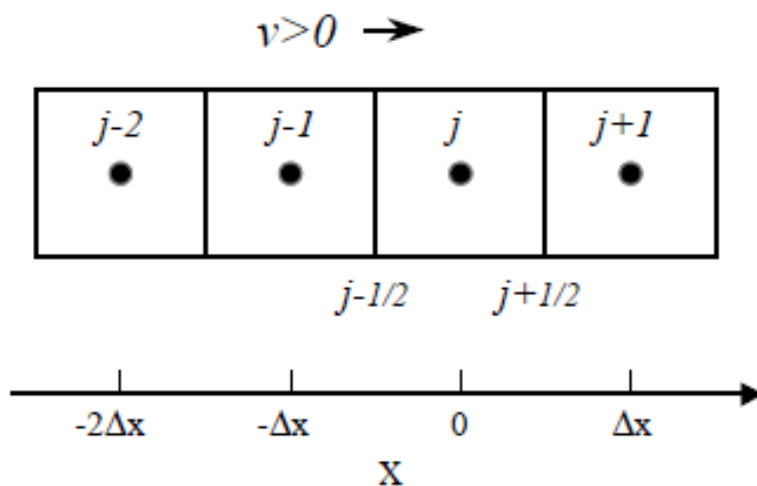
3. kinetic deposition and detachment terms and blocking:

➤ Best-fit parameters are  $K_{\text{dep}}$ ,  $K_{\text{det}}$  and  $S_{\max}$

$$r_{\text{dep}} = \rho_b \frac{\partial S}{\partial t} = nK_{\text{dep}}\psi C - \rho_b K_{\text{det}} S \quad \psi = (1 - S/S_{\max}) \quad 14$$

# TVD Numerical Scheme

- TVD methods are **Eulerian** methods and, hence, are inherently based on the principle of mass conservation.
- In TVD based methods, the interface concentrations are estimated using **higher-order** (e.g., third-order) polynomial interpolation of the nodal concentrations.



$$C_{j+1/2} = (C_{j+1} + C_j)/2 - C_r (C_{j+1} - C_j)/2 - (1 - C_r^2)(C_{j+1} - 2C_j + C_{j-1})/6$$

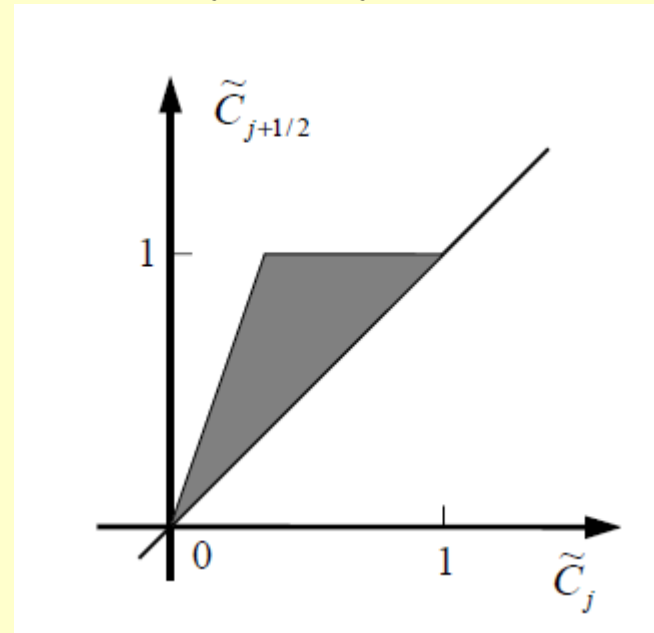
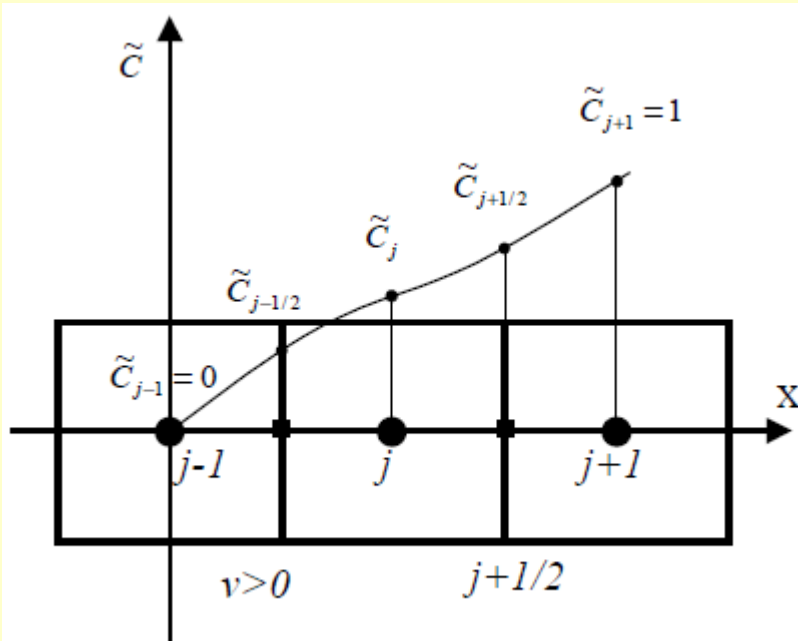
and

$$C_{j-1/2} = (C_j + C_{j-1})/2 - C_r (C_j - C_{j-1})/2 - (1 - C_r^2)(C_j - 2C_{j-1} + C_{j-2})/6$$

where  $C_r = v\Delta t/\Delta x$

# TVD Numerical Scheme (continued)

- TVD method utilizes a **universal flux limiting** procedure to minimize unphysical oscillations that may occur particularly when sharp concentration fronts are present.
- In order to ensure that the concentration profile is locally monotonic, interpolated concentrations at the interface (say  $j+1/2$ ) must fall within the shaded area.
- If not, the concentration at the interface is set equal to the concentration of the closest upstream node  $C_{j+1/2} = C_j^n$





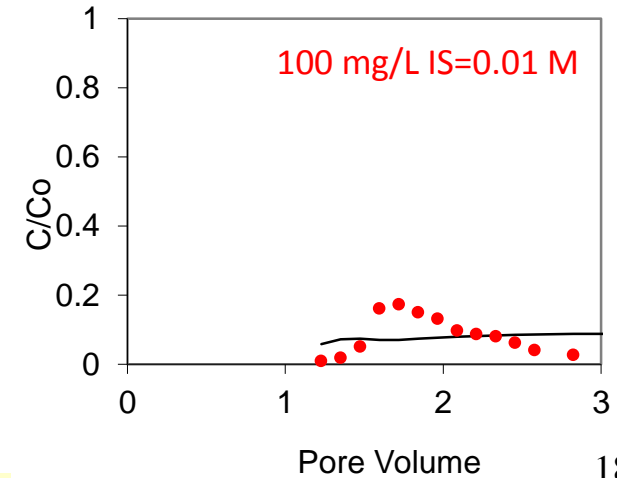
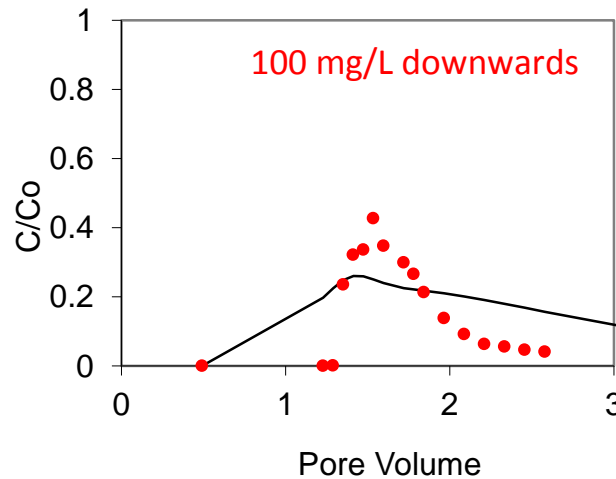
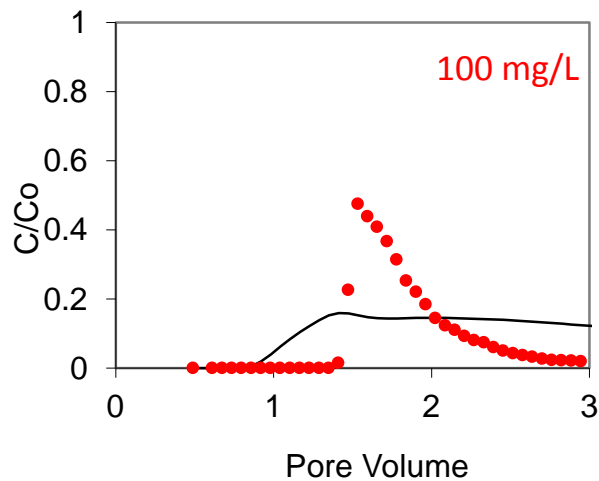
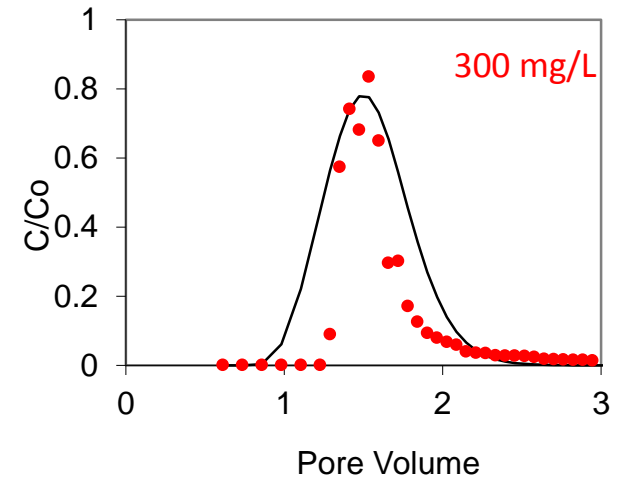
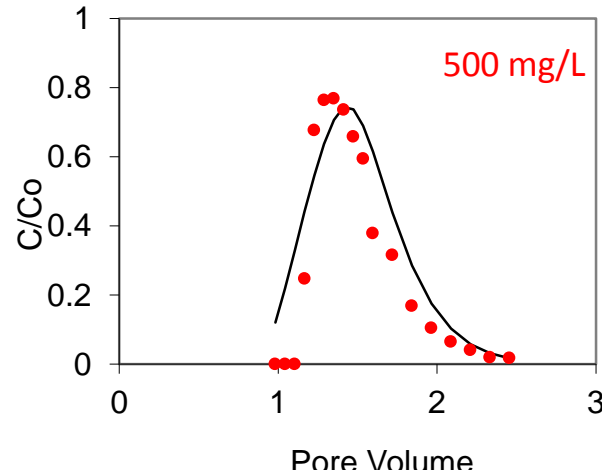
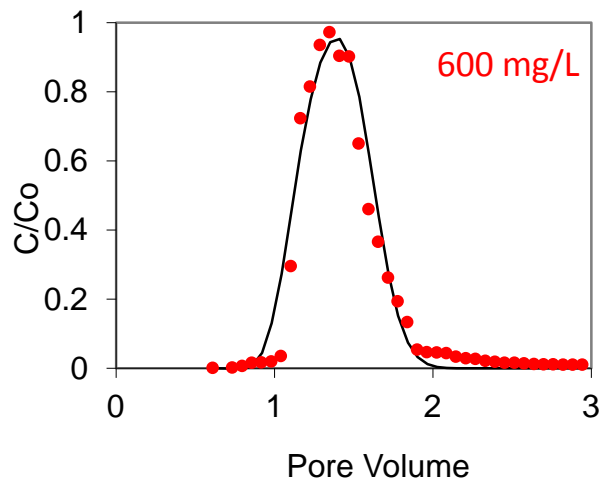
# Parameter Estimation Scheme

---

- For the estimation of the transport parameters, the transport model was coupled with, an optimization algorithm, a modified [Levenberg-Marquardt algorithm \(LMA\)](#).
- LMA is a non-linear least-squares estimator. It uses an iterative technique to minimize the difference squared between the observed and simulated concentrations.
- The Jacobian, which is needed for the estimation of the next iteration of the parameters, is estimated using a finite-difference method.
- LMA finds a local minimum. Therefore, to ensure proper convergence, different initial values of the parameters were considered.

# Simulated vs Observed Concentrations Histories

## 1. kinetic deposition and detachment but no blocking (large $S_{\max}$ )



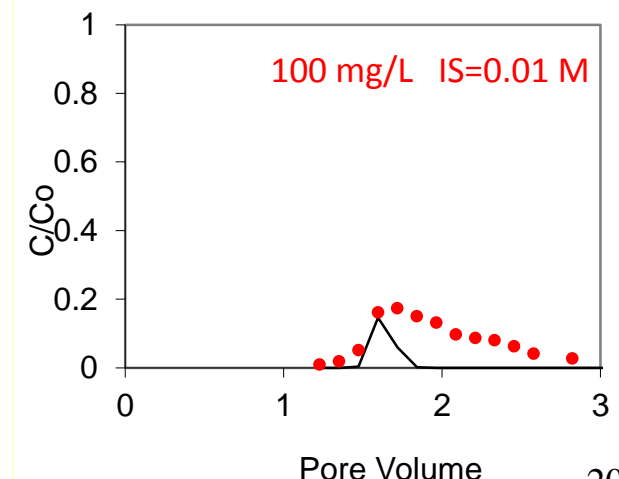
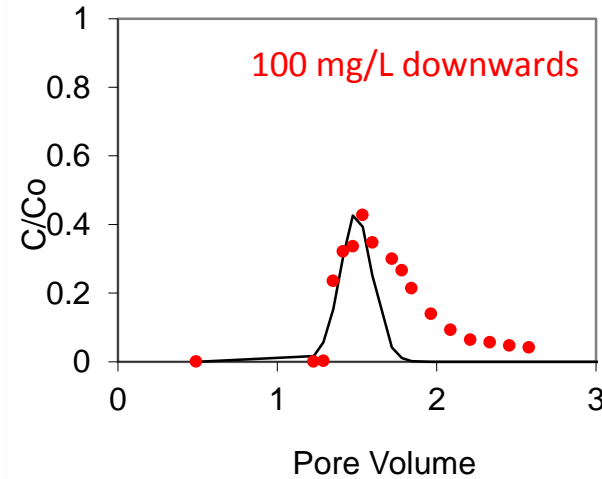
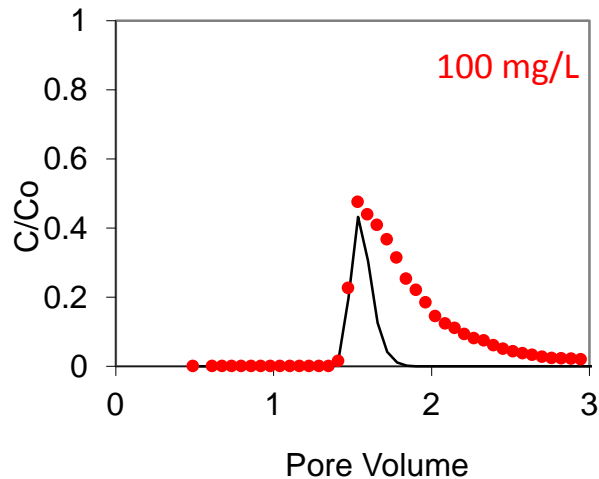
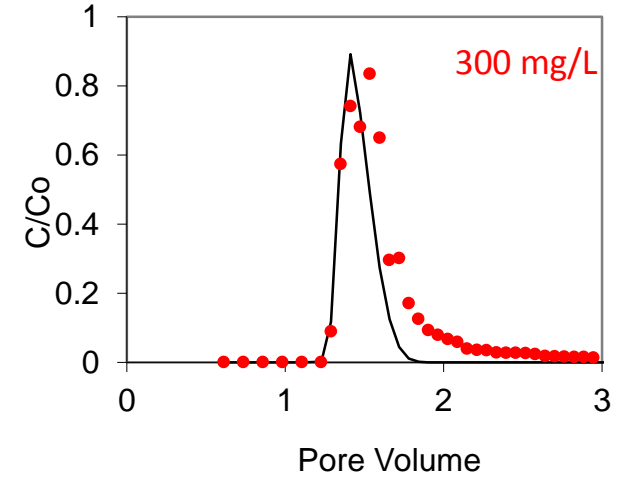
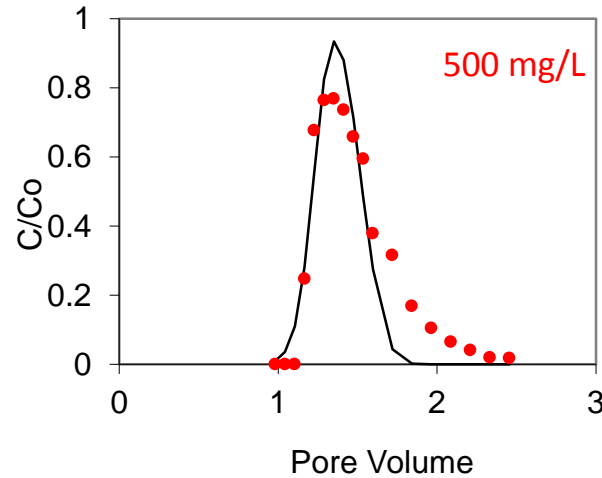
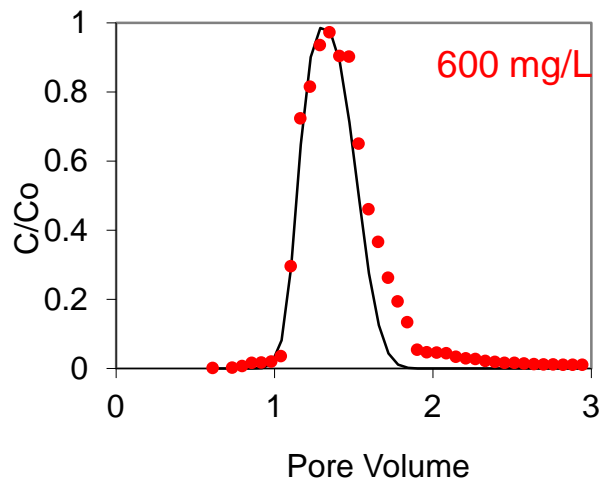
# Best-fit Model Parameters Constants

## 1. kinetic deposition and detachment but no blocking (large $S_{\max}$ )

Test	Input Fe (mg/L)	$S_{\max}$ mg/g	$K_{dep}$ min <sup>-1</sup>	$K_{det}$ min <sup>-1</sup>	$R^2$
2	600	-	0.18	0.60	0.96
3	500	-	0.68	0.11	0.84
4	300	-	0.14	0.20	0.76
5	100	-	0.093	0.017	0.21
6	100 (downward flow)	-	0.078	0.024	0.46
7	100 (0.01 M IS solution)	-	0.12	0.012	0.05

# Simulated vs Observed Concentrations Histories

## 2. kinetic deposition with blocking but no detachment ( $K_{det} = 0$ )



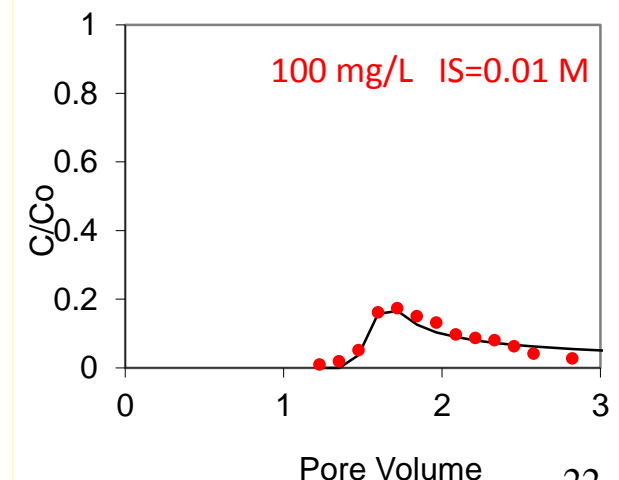
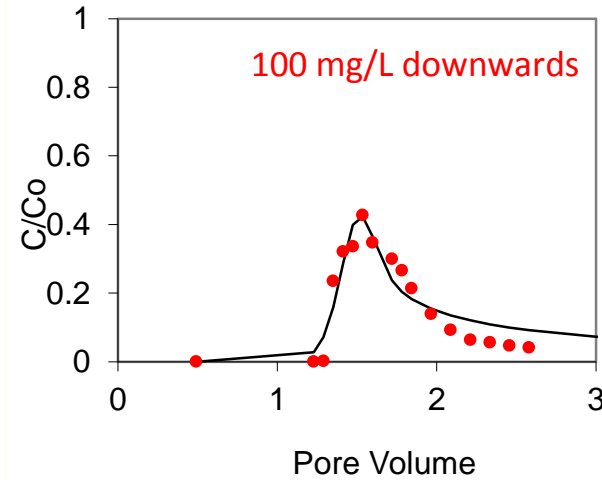
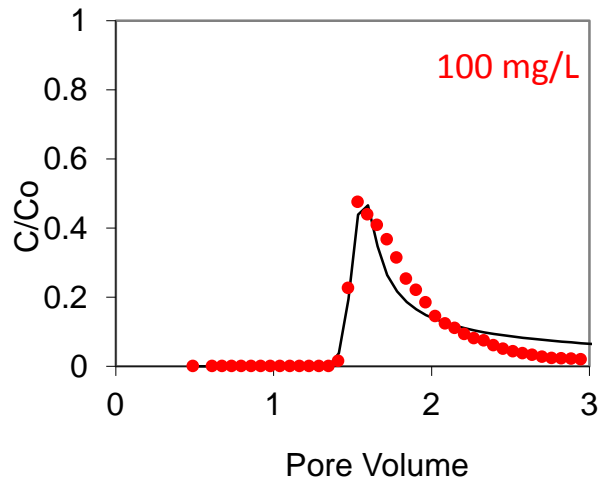
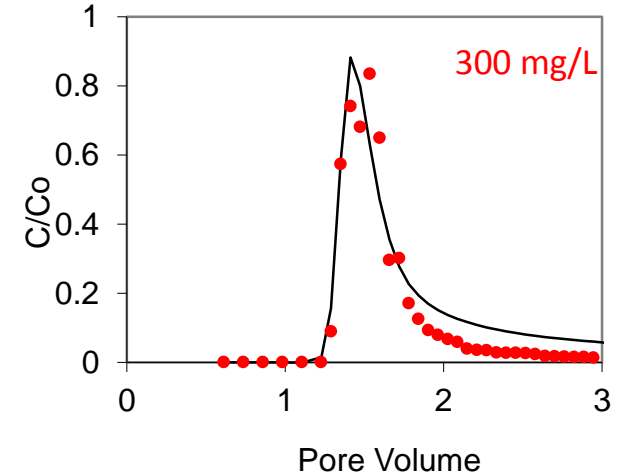
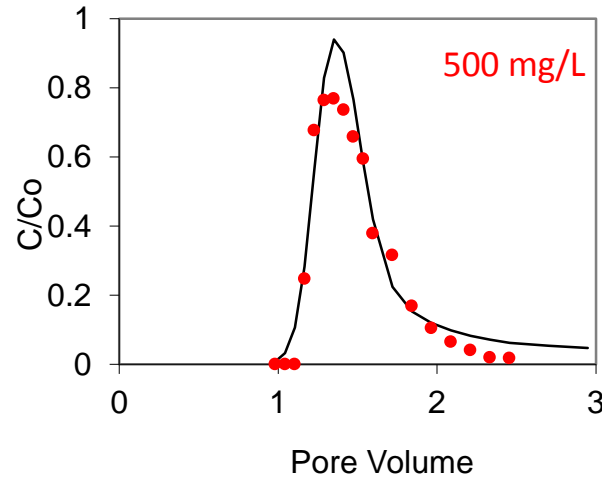
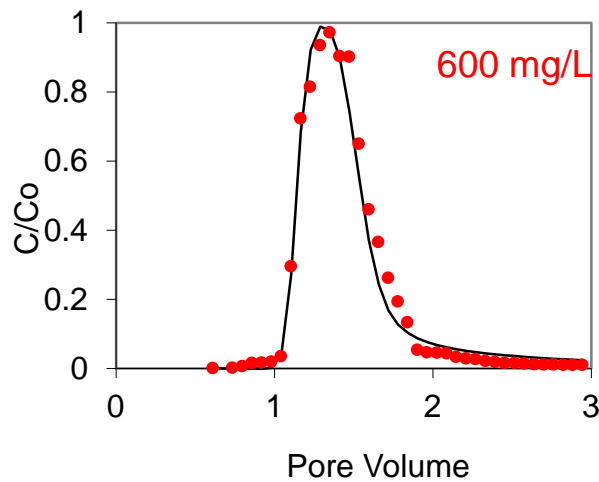
# Best-fit Model Parameters Constants

## 2. kinetic deposition with blocking but no detachment ( $K_{det} = 0$ )

Test	Input Fe (mg/L)	$S_{max}$ mg/g	$K_{dep}$ min <sup>-1</sup>	$K_{det}$ min <sup>-1</sup>	$R^2$
2	600	0.039	0.26	-	0.95
3	500	0.052	0.21	-	0.90
4	300	0.051	1.6	-	0.82
5	100	0.024	2.6	-	0.54
6	100 (downward flow)	0.022	0.40	-	0.61
7	100 (0.01 M IS solution)	0.027	5.6	-	0.35

# Simulated vs Observed Concentrations Histories

## 3. kinetic deposition and detachment with blocking



# Best-fit Model Parameters Constants

## 3. kinetic deposition and detachment with blocking

Test	Input Fe (mg/L)	$S_{\max}$ mg/g	$K_{dep}$ min <sup>-1</sup>	$K_{det}$ min <sup>-1</sup>	$R^2$
2	600	0.041	0.50	0.053	0.98
3	500	0.055	0.24	0.032	0.95
4	300	0.054	1.0	0.053	0.93
5	100	0.026	1.5	0.030	0.93
6	100 (downward flow)	0.024	0.33	0.013	0.90
7	100 (0.01 M IS solution)	0.028	1.2	0.040	0.91

# Summary and Conclusions

---

- Laboratory-scale transport experiments revealed that PAA-supported magnetite NP mass recovery from the column decreased consistently with decrease in input concentration.
- A NP transport model that accounts for advection, hydrodynamic dispersion as well as deposition/detachment kinetics suggest that the decrease in mass recovery with decrease in particle concentration may be due to time-dependent blocking which hinders further deposition.
- The dependence of NP mobility on input concentration suggests that in real applications NP transport efficiency and reaction potential may decrease with travel distance as the injected NP remedial solution is diluted.



# Acknowledgements

---

## Colleagues:

**Dila Aksoy, Asu Ziylan, Nilsun H. Ince**

*Institute of Environmental Sciences, Bogazici University,  
Istanbul, Turkey*

**Havva Yagci Acar, Miray Demirer**

*Department of Chemistry, Koç University, Istanbul, Turkey*

## Financial Support:

**TÜBİTAK- The Scientific and Technology Research  
Council of Turkey**

Thank you

---



Institute of Environmental Sciences  
Bogazici University  
Istanbul, Turkey

